

Measuring the Higgs-bottom coupling in weak boson fusion

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We study Higgs production through weak boson fusion with subsequent decay to bottom quarks. By combining jet substructure techniques and matrix element methods in different limits we motivate this channel as a probe of the bottom-Yukawa interactions in the boosted regime. In particular we ameliorate the “no-go” results of cut-and-count analyses in this channel. After applying a data-driven reconstruction approach we find that the Higgs-bottom coupling can be limited to $0.82 < y_b/y_b^{\text{SM}} < 1.14$ with 600 fb^{-1} .

I. INTRODUCTION

After the Higgs discovery [1, 2] and a growing consistency of Higgs measurements by ATLAS and CMS with the Standard Model (SM) hypothesis [3], diversifying and extending Higgs to all available production and decay channels is of utmost importance. On the one hand, this strategy will allow us to over-constrain fits to, e.g., the dimension six extension of the Higgs sector, or, on the other hand, could facilitate a new physics discovery in non-standard and less “traditional” Higgs search channels.

The coupling of the Higgs boson to bottom quarks is outstandingly important in this regard, because we expect a Higgs decay to bottom final states at around 60% [4]. Yet, none of the currently available analyses is directly sensitive to this coupling. Even the smallest deviation of the Higgs coupling to bottom quarks has far reaching consequences for the Higgs lifetime; a modification of which might, e.g., point to a possible relation of the TeV scale with a hidden sector. Since a modified Higgs phenomenology can arise from multiple sources, fingerprinting the bottom Yukawa interaction is mandatory to experimentally verify mass generation of the third generation down sector, especially because the standard ways of looking for Yukawa interactions such as Higgs production or bottom-quark associated Higgs production suffer either from dominant virtual top-quark contributions or a small total rate in light of a huge background.

In fact, there are only a few processes that contribute to a direct measurement of the bottom-Yukawa coupling: associated Higgs production [5–7] and top-associated Higgs production [8–10], with subsequent decay $H \rightarrow b\bar{b}$, both of which are challenging to probe at the LHC, even with large statistics.

It is the purpose of this work to add another sensitive channel to this list: weak boson fusion (WBF)-like Higgs

production with decay to bottom quarks. This channel has been studied in Ref. [11], which quoted a very small signal vs background ratio, effectively removing this process from the list of interesting Higgs processes. This is mainly due to large backgrounds and little handle (such as a missing central jet veto [12–14]) to control them. In this work we extend the analysis of [11] by employing novel reconstruction and all-information approaches through combining shower deconstruction [15, 16], an all-order matrix element method to analyse fat jets, with the fix-order matrix element method techniques [17, 18] for the hard process. We show that the large backgrounds can be significantly reduced, while a major part of the signal can be retained. This allows us to ameliorate the no-go expectation of “traditional” cut-and-count analyses for WBF Higgs production with b -quark final states.

This work is organised as follows. In Sec. II, we comment on our event generation and the used analysis tools. Specifically, we review the matrix element method and shower deconstruction in Secs. II B and II C to make this work self-contained. Sec. III is devoted to our results. We perform a naive cut-and-count analysis and show that kinematic handles alone do not provide enough discriminating power to sufficiently isolate signal from background. We show that the latter can be achieved with a combination of matrix element method and shower deconstruction techniques, leading to an expected sensitivity to the SM WBF contribution with around 100 fb^{-1} luminosity. Sec. IV provides a summary and gives our conclusions.

II. EVENT GENERATION AND ANALYSIS TOOLS

A. Event generation

We generated events at Leading Order in the four flavor scheme with MadGraph5_aMC@NLO [19–21]/Pythia8.2 [22] using NNPDF2.3 [23] for the parton distribution functions. The generation was split into five independent samples: two for the signal and four for the background. The two signal samples are the Higgs production in as-

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sociation with two light jet via either weak boson fusion (WBF) or via gluon fusion (GF) with the Higgs decaying into a $b\bar{b}$ pair. The gluon fusion process was generated via the new extension of `MadGraph5_aMC@NLO` supporting loop induced processes [24] and include the full top and bottom mass effects. For the background we split the $b\bar{b}jj$ final state into pure QCD production (referred to as $b\bar{b}jj$) and electroweak production (referred to as Zjj). The last background sample is the four light-flavor jet sample ($jjjj$), for which we limit ourself to the pure QCD contribution. To avoid the double counting between the $jjjj$ and the $b\bar{b}jj$ samples related to b emission in the parton-shower, we ran a four flavor parton-shower for the $jjjj$ sample.

At parton level a couple of loose cuts are applied in order to gain in efficiency. For all the samples with two b quarks and two light jets in the final state, we apply the following cuts:

$$\begin{aligned} p_{T,b} &\geq 20 \text{ GeV}, \\ p_{T,j} &\geq 35 \text{ GeV}, \\ y_{j_1} \cdot y_{j_2} &< 0, \\ |y_{j_1} - y_{j_2}| &> 3.0, \\ m_{j_1,j_2} &\geq 500 \text{ GeV} \\ o_{T,(b+\bar{b})} &\geq 150 \text{ GeV}, \\ \Delta R_{all,all} &\geq 0.2. \end{aligned}$$

For the $jjjj$ sample, the same cuts are applied with the index “ j_1, j_2 ” being identified as the two most forward jets and the index “ b ” refers to the two central jets.

B. The Matrix Element method

The matrix element method [17, 18] is based on the Neyman-Person Lemma [25] stating that the best discriminant variable is the likelihood ratio where the likelihood is the product of probabilities evaluated on the sample. The probability of an event is computed in the matrix element method by calculating

$$\mathcal{P}_\alpha(p^{exp}) = \frac{1}{\sigma} \int d\Phi(p^{part}) |M_\alpha(p^{part})|^2 P(p^{exp}|p^{part}),$$

where p^{exp} represents the measured momenta for a given event, p^{part} is the partonic phase-space point which we integrate over with a phase-space measure $d\Phi(p^{part})$ that also includes the parton distribution functions. $|M_\alpha(p^{part})|^2$ is the matrix element square for a given hypothesis α and $P(p^{exp}|p^{part})$, named the transfer functions, is the conditional probability to observe the experimental event under consideration for a given partonic phase-space point.

Using the best discriminant variable allows us to perform measurements for processes with extremely small cross-section or small event rate. However, even if the above integral can be computed via dedicated tools [26],

this is very CPU intensive when performed for the full sample of events. In order to analyse large background samples efficiently, we therefore simplify the method by approximating the transfer function by a delta function, allowing us to drop the computation of the integral entirely [15, 27]. This is conservative, since including such effect can only improve the sensitivity of the method*.

Therefore, for each event, the matrix element method is equivalent to computing the following likelihood ratio:

$$\chi_{MEM} = \frac{|M_{wbf}|^2 + |M_{gf}|^2}{|M_{jjjj}|^2 + |M_{bbjj}|^2 + |M_{Zjj}|^2}. \quad (1)$$

For additional speed efficiency, the gluon fusion matrix element is not computed using the one loop matrix element – like we did for the event generation – but at tree level with an effective vertex coming from the integrating out the top quark loop [30]. The signal matrix elements (GF and WBF) are computed for a three body final state (with the Higgs momentum being identified with the reconstructed $b\bar{b}$ -pair momentum) while the backgrounds are computed for the four particle final state using the tagged b subjet from the fat jet (see Sec. III). To avoid potential bias, we use a different sets of PDFs for the analysis (CT10 [31]) compared to the one used for the event generation.

C. Shower Deconstruction

Shower deconstruction [15, 16] is an all-order matrix element method designed to discriminate hadronically decaying electroweak-scale resonances, i.e. tops, W/Z or Higgs boson, from QCD jets. First the constituents of a fatjet are reclustered into small inclusive jets, e.g. using the k_T jet algorithm [32] with $R=0.2$ and $p_{T,j} > 5$ GeV. One obtains a configuration of N subjets with four-momenta $\{p\}_N = \{p_1, p_2, \dots\}$. Using these subjets as input to the method, a likelihood ratio is calculated from first-principle QCD, quantifying whether the observed distribution of subjets was initiated by the decay of a signal process, e.g. a Higgs boson, or background, e.g. a gluon. To calculate the likelihood ratio

$$\chi_{SD}(\{p\}_N) = \frac{P(\{p\}_N|S)}{P(\{p\}_N|B)}, \quad (2)$$

where $P(\{p\}_N|S)$ represents the probability of obtaining the subjet distribution $\{p\}_N$ given the signal hypothesis, and $P(\{p\}_N|B)$ is the probability for obtaining the same $\{p\}_N$ from background processes. To calculate $P(\{p\}_N|B)$ and $P(\{p\}_N|S)$ the method sums over all possible shower histories. In [33] it was shown that χ_{SD} is insensitive to pileup and shows good agreement

*Further improvements could be achieved by evaluating the matrix elements at NLO accuracy [28, 29].

between data and Monte-Carlo prediction. We follow loosely the approach described in [34] to combine shower deconstruction with the fix-order matrix element method of Sec. II B.

III. RESULTS

Based on the event generation detailed above, we first establish a baseline cut scenario inspired by [11, 35].

In the first step, we veto events with isolated leptons with $|y_l| \leq 2.5$ and $p_{T,l} > 10$ GeV. We then request a $R = 1.2$ Cambridge-Aachen [36] fat jet[†] with

$$\begin{aligned} p_{T,j_{\text{fat}}} &> 200 \text{ GeV}, \\ |y_{j_{\text{fat}}}| &< 2.5, \\ \text{and } m_{j_{\text{fat}}} &> 90 \text{ GeV}. \end{aligned} \quad (3)$$

After having identified a fat jet, we remove its constituents from the final state, and the remaining constituents in the event are clustered using anti- k_T $R = 0.6$ jets [38] with $p_{T,j} > 50$ GeV in $|y_j| < 4.5$. The two jets with largest rapidity we define as so-called tagging jets j_1 and j_2 .

In the next step, we impose typical and stringent WBF selection requirements on these two tagging jets; they need to have a large invariant mass, are required to lie in different detector hemispheres, and need to be separated by a large rapidity gap

$$\begin{aligned} m_{j_1,j_2} &\geq 1000 \text{ GeV}, \\ y_{j_1} \cdot y_{j_2} &< 0, \\ |y_{j_1} - y_{j_2}| &> 4.0. \end{aligned} \quad (4)$$

The first cut in particular decreases the gluon fusion contribution significantly which is a necessary requirement to end up with the clean WBF-like selection to separate the impact of new physics between the two production modes [27].

The typical WBF $pp \rightarrow hjj$ event topology that we want to isolate is a Mercedes star configuration. Hence, we veto events for which one of the tagging jets is central or collimated to the fat jet, i.e. we require

$$\begin{aligned} |y_{j_{1,2}}| &\geq 2.5 \\ \Delta\phi(j_{\text{fat}}, j_{(1,2)}) &> 2.0. \end{aligned} \quad (5)$$

in the third step of the analysis.

Since the fat jet is produced centrally, we cannot use generic ways to reduce the hadronic backgrounds, such as central/mini-jet vetos which would also push the gluon fusion contribution to the percent level.

In the last step, we turn to the fat jet that we removed earlier from the event record. We recombine the constituents of the fat jet to so-called microjets with $R = 0.2$

and $p_{T,j_m} \geq 5$ GeV. Of these microjets we require the two with largest transverse momentum to be b -tagged. We assume a flat 60% tagging efficiency and 1% fake rate. To facilitate a b -tag, the microjets need to have $p_{T,j_m} \geq 15$ GeV. We decay the B -mesons, do not account for missing energy in the reconstruction (hence our result is conservative), and, in addition to the assumed tagging efficiency, for a b -tag we match the B -meson to the respective jet by requiring $\Delta R_{B_{\text{mes}},j} < R$.

A cut flow of our analysis is shown in Tab. I; distributions of signal and backgrounds are shown in Fig. 1. It is important to realise that after step (iii) we have exhausted all kinematic handles to suppress the backgrounds and find ourselves in the unfortunate situation that b -tagging is not discriminative enough to cure a bad signal vs. background ratio.[‡] Increasing the invariant mass cut would lead to a further suppression of the backgrounds, however at an unacceptably large decrease of the signal yield, leading to a vanishing sensitivity to WBF.[§]

With all “traditional” means exhausted we are left with two approaches: (i) reverting to multivariate techniques such as boosted decision trees or neural networks which heavily rely on the treatment of systematics and training, combining a few observables that still show promise to increase signal over background (see e.g. the recent Ref. [40]), or (ii) improve the analysis in a way that is motivated by the asked physics question. The latter avenue is exactly provided by combining the matrix element method for the hard process with shower deconstruction, a matrix element method for soft and collinear QCD radiation. The former provides a statistical discrimination on the basis of expected signal and background contributions, while the latter isolates the $H \rightarrow b\bar{b}$ decay from the irreducible backgrounds by comparing the different shower histories.

We separately calculate χ_{SD} of Eq. (2) and χ_{MEM} of Eq. (1), see Fig. 2. Again, this approach is conservative, as the sensitivity of the analysis can be increased by combining shower deconstruction and the matrix element method, see [34] for a discussion. The two-dimensional correlation of matrix element method and shower deconstruction isolates a region of phase-space with a maximum signal-over-background ratio of 1/13.9, requiring at least 3 signal events in isolated bins at 100/fb. Since shower deconstruction can highly discriminate between $H \rightarrow b\bar{b}$ and the continuum background, by integrating over adjacent bins in the shower deconstruction observable, we obtain this way 10 events for 100/fb at a reduced signal vs. background ratio of 1/28.8. While this consti-

[†]Jet finding and clustering is performed with FASTJET [37].

[‡]We have checked that the top pair background also contributes ~ 3 fb at this stage, but becomes completely negligible in the matrix element method+shower deconstruction signal region detailed below.

[§]Our results in this regard are compatible with the earlier results of Ref. [11].

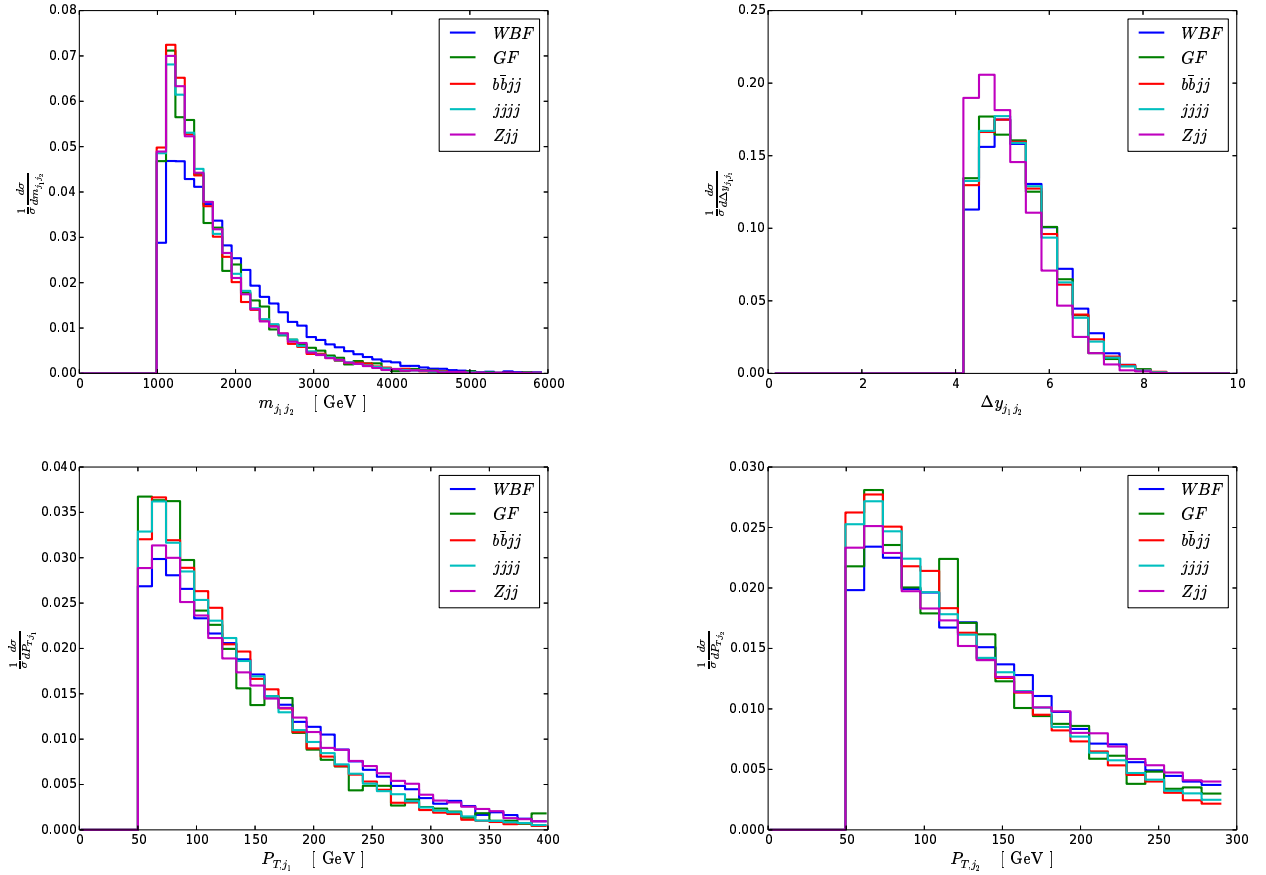


FIG. 1: Representative kinematic distributions of signal and background processes after the analysis steps described in Sec. III have been carried out.

		WBF	GF	$b\bar{b}jj$	Zjj	$jjjj$
(i)	fat jet	48.50	17.32	205109	553.16	$2.23 \cdot 10^7$
(ii)	wbf cuts	21.23	4.11	48441.9	127.98	$5.18 \cdot 10^6$
(iii)	mercedes star	18.44	2.82	31674.5	84.975	$3.39 \cdot 10^6$
(iv)	fatjet b -tags	4.59	0.578	3800.99	12.57	323.74

TABLE I: Cut flow of the cut-based analysis described in Sec. III. The steps (i)-(iii) show the cross sections after the cuts of Eqs. (3)-(5). Cross sections are quoted in units of femtobarns.

tutes a tremendous improvement over the cut and count analysis with $S/B \simeq 1/800$, it is still obvious that background systematics can have a significant impact.

Since this would render a likelihood analysis of the matrix element method-shower deconstruction correlation unreliable, we instead turn to a data driven approach based on pre-selecting a matrix element likelihood regime favored by the signal and fitting the background distribution of the shower deconstruction output. In practice, a fit based on a product of a Gaussian and a polynomial of degree 2

$$f(x) = (ax^2 + bx + c) \exp[d(x - x_0)^2] \quad (6)$$

with fitted parameters a, b, c, d, x_0 works very well as the background template with $x = \log(\chi_{SD})$, see Fig. 3. This opens the possibility to perform a search for the Higgs boson similarly to the search for the Higgs in other channels under the conditions that the background is not very well understood, leading to large systematics once theoretical uncertainties are treated at face value: one uses a background fit function that is motivated from MC analysis to fit the distribution, which then has small systematic uncertainty and looks for enhancements over the expected background model. With increased statistics the fit quality becomes better and systematic uncertainties become negligible quickly (again similar to the situation

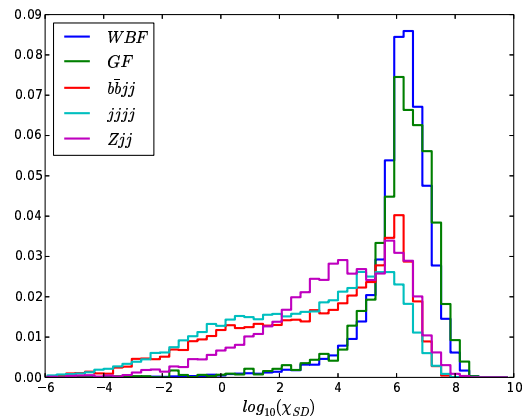
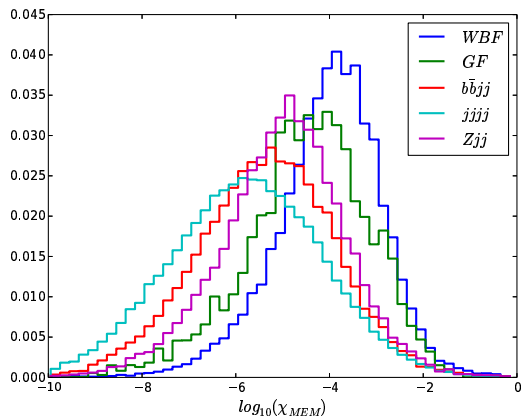


FIG. 2: Distribution of events for both the matrix element method likelihood ratio (left) and shower deconstruction (right) after the analysis steps described in Sec. III have been carried out.

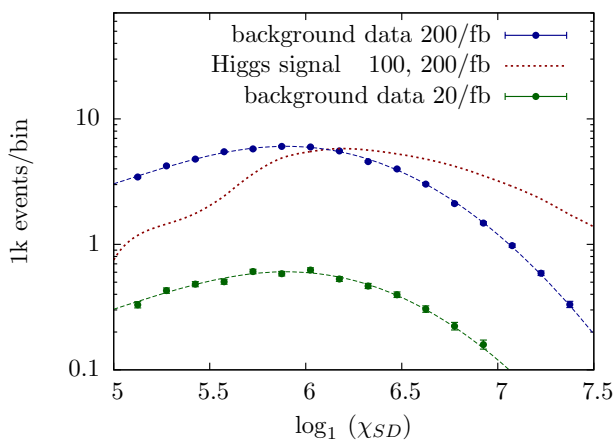


FIG. 3: Expected background distribution of the shower deconstruction output for luminosities of 20 fb^{-1} and 200 fb^{-1} . Note that the statistical uncertainty becomes negligible. For the 200 fb^{-1} case we also compare the background fit to the Higgs signal distribution (multiplied by a factor 100). Exploiting the different shape of the signal above a well-modeled background is key to the limit setting described in the text. The (asymmetric) error bars on each bin are calculated using quantiles following the ATLAS statistics recommendations [41] inputting the expected background count.

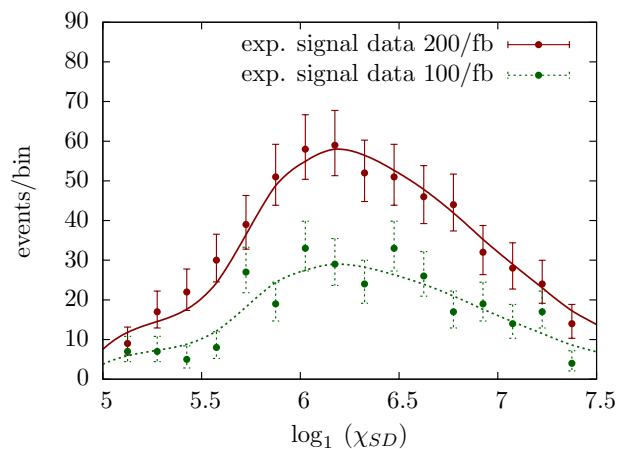


FIG. 4: Expected signal distribution of the shower deconstruction output for 100 and 200 fb^{-1} . We also plot signal pseudo-data to highlight the expected scatter of the signal events for the ideal scenario of a perfect background fit. The (asymmetric) error bars on each bin are calculated using the ATLAS statistics recommendations [41] inputting the expected signal count.

in $H \rightarrow \gamma\gamma$ searches). Concretely we find the signal to be clustered around $\log(\chi_{SD}) \simeq 6$ while the background distribution is a smooth Gaussian-like distribution of Eq. (6) in the search region $\log(\chi_{SD}) > 5$.

At a luminosity $\lesssim 100 \text{ fb}$ the total number of signal events, as well as the different shape of the signal distribution, Figs. 3 4, become resolvable on the basis of the binned log likelihood method of [39, 42]. (we stress again that the error bars in Figs. 3 and 4 are purely exemplary; the correct combined background+signal distributions are sampled in using the methods of [39, 42] and taken into account in the limits we quote). This means

we can start excluding the SM at 95% confidence level in case the Higgs has a suppressed bottom Yukawa interaction. On the other hand, assuming a SM-like Higgs boson, we can turn this exclusion into a coupling measurement. Projecting to 600 fb^{-1} , we obtain a constraint

$$0.82 < y_b/y_b^{\text{SM}} < 1.14$$

at 95% confidence level by propagating the impact of the modified bottom Yukawa interaction through the Higgs production and decay phenomenology while keeping all other Higgs couplings fixed to their SM values.

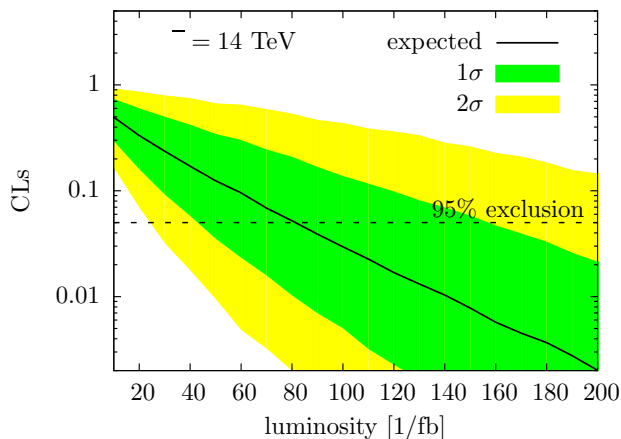


FIG. 5: Expected exclusion using the CLs method [39] based on the data-driven analysis. For details see text.

IV. SUMMARY AND CONCLUSIONS

In this paper we have performed an analysis of Higgs production via weak boson fusion (WBF) with subsequent decays $H \rightarrow b\bar{b}$. While this process is heavily plagued with backgrounds due to the non-availability of signal vs background enhancing strategies like the cen-

tral jet veto, we have shown that by combining novel analysis strategies, we can elevate the discouraging result of a simple cut-and-count analysis that exploits the basic kinematic features of WBF to a sensitive strategy at a luminosity of about 100 fb^{-1} . Our strategy has the additional advantage that it relies on a data-driven fit of the background template, which is derived from first principle QCD and fixed-order calculations instead of relying on nontransparent multivariate techniques. Crucial to this strategy is that the matrix element method and shower deconstruction combine complementary information - an analysis solely based on one of these tools does not provide enough discriminating power to increase the sensitivity to WBF Higgs production in the bottom final state. As a result, during the upcoming run of the LHC, ATLAS and CMS will be able to probe the Higgs-bottom coupling in a complementary way to well established measurements in $t\bar{t}H$ and VH .

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